

**Dr Oliver Mathematics**  
**GCSE Mathematics**  
**2023 June Paper 1H: Non-Calculator**  
**1 hour 30 minutes**

The total number of marks available is 80.

You must write down all the stages in your working.

1. Work out (3)

$$8.46 \div 0.15.$$

2. Work out (3)

$$7\frac{3}{8} - 2\frac{1}{2}.$$

Give your answer as a mixed number.

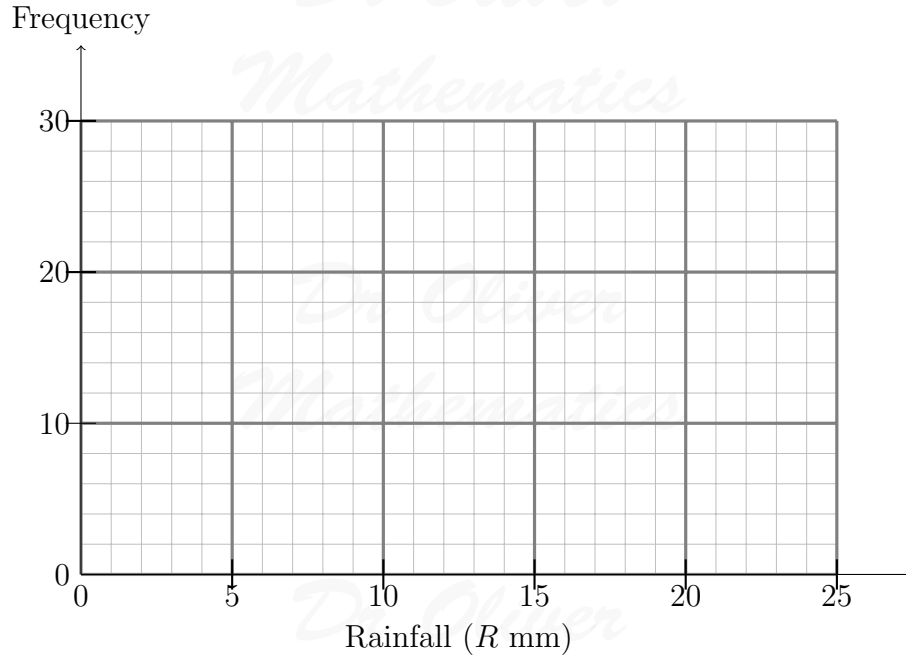
3. A cube has a total surface area of  $150 \text{ cm}^2$ . (4)

Work out the volume of the cube.

4. The table shows information about the daily rainfall in a town for 60 days. (2)

Rainfall ( $R$ mm)	Frequency
$0 \leq R < 5$	8
$5 \leq R < 10$	24
$10 \leq R < 15$	13
$15 \leq R < 20$	11
$20 \leq R < 25$	4

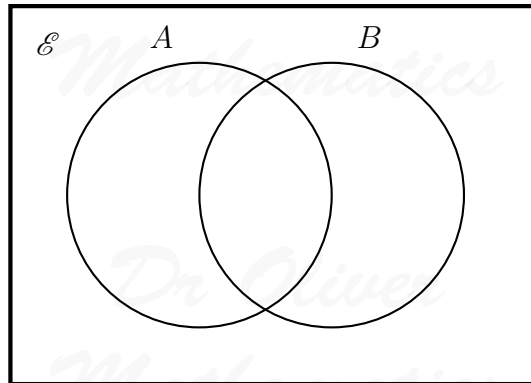
Draw a frequency polygon for this information.



5. •  $\mathcal{E} = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ .  
 •  $A = \{\text{odd numbers}\}$ .  
 •  $B = \{\text{square numbers}\}$ .

(a) Complete the Venn diagram for this information.

(3)

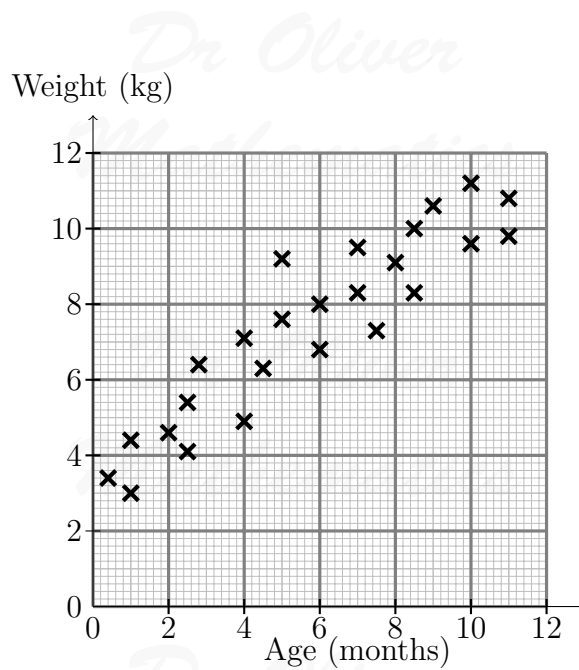


A number is chosen at random from the universal set  $\mathcal{E}$ .

(b) Find the probability that this number is in the set  $B'$ .

(2)

6. The scatter graph shows information about the ages and weights of some babies.



(a) Describe the relationship between the age and the weight of the babies. (1)

Another baby has a weight of 5.8 kg.

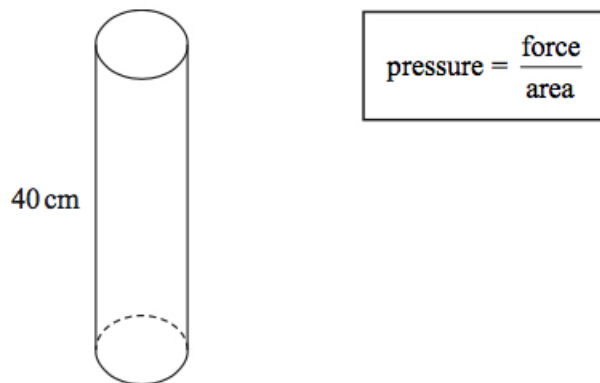
(b) Using the scatter graph, find an estimate for the age of this baby. (2)

7. The price of a holiday increases by 20%. (2)

This 20% increase adds £240 to the price of the holiday.

Work out the price of the holiday before the increase.

8. The diagram shows a solid cylinder on a horizontal floor. (3)



The cylinder has a

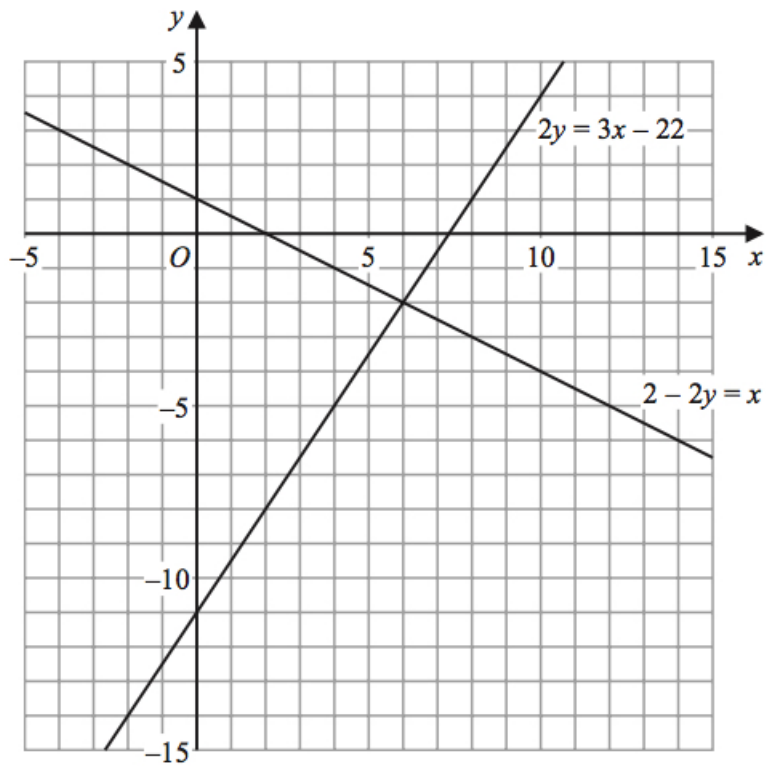
- volume of  $1\,200\text{ cm}^3$  and

- height of 40 cm.

The cylinder exerts a force of 90 newtons on the floor.

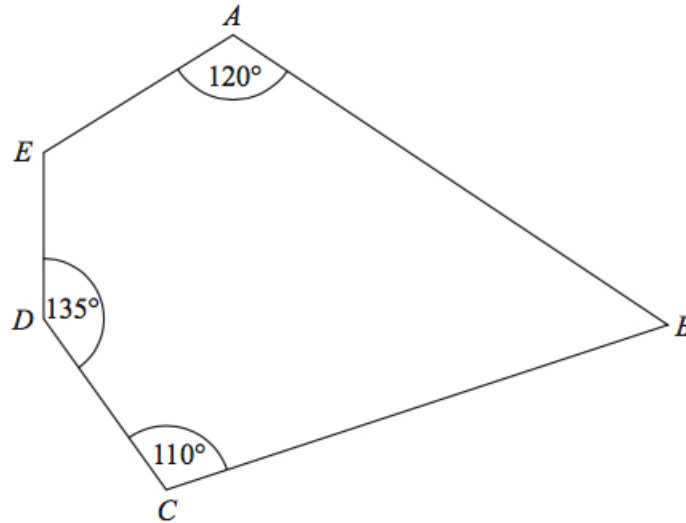
Work out the pressure on the floor due to the cylinder.

9. Use these graphs to solve the simultaneous equations (1)



$$\begin{aligned} 2 - 2y &= x \\ 2y &= 3x - 22. \end{aligned}$$

10. Here is a pentagon (4)



Angle  $AED = 4 \times \text{angle } ABC$ .

Work out the size of angle  $AED$ .  
You must show all your working.

11. Write (3)

$$\frac{(6x^5y^3)^2}{3x^2y^7 \times 4xy^{-3}}$$

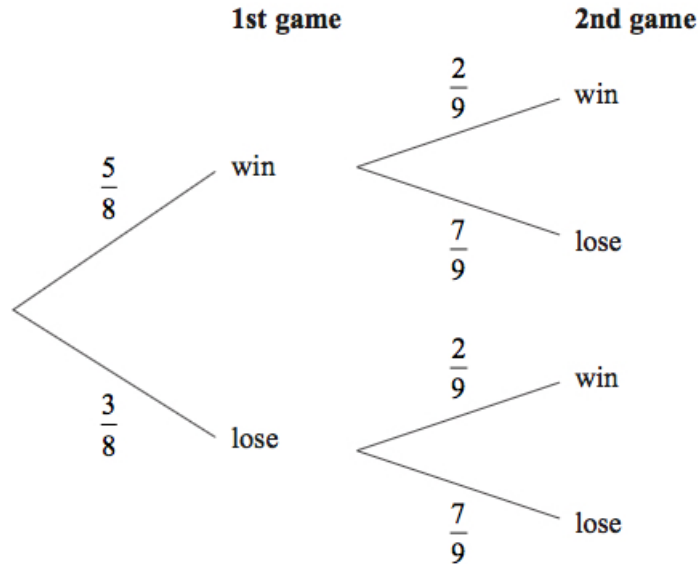
in the form

$$ax^by^c,$$

where  $a$ ,  $b$ , and  $c$  are integers.

12. Martha plays a game twice. (3)

The probability tree diagram shows the probabilities that Martha will win or lose each game.



Find the probability that Martha will lose at least one game.

13.  $y$  is directly proportional to  $x$ . (3)

$y = 24$  when  $x = 1.5$ .

Work out the value of  $y$  when  $x = 5$ .

14. (a) Write  $\frac{1}{16}$  in the form  $4^n$  where  $n$  is an integer. (1)

- (b) Work out the value of (3)

$$8^{\frac{5}{3}} - 9^{\frac{3}{2}}$$

15. The equation of line  $L_1$  is  $y = 2x - 5$ . (3)

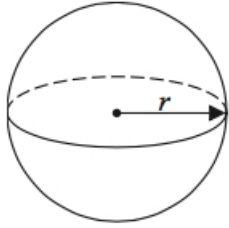
The equation of line  $L_2$  is  $6y + kx - 12 = 0$ .

$L_1$  is perpendicular to  $L_2$ .

Find the value of  $k$ .

You must show all your working.

16. Here is a sphere. (4)



Surface area of sphere = $4\pi r^2$
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$\frac{3}{8}$  of the surface area of this sphere is  $75\pi \text{ cm}^2$ .

Find the diameter of the sphere.

Give your answer in the form  $a\sqrt{b}$ , where  $a$  is an integer and  $b$  is a prime number.

17. Make  $x$  the subject of the formula

(4)

$$y = \frac{4(2x - 7)}{5x + 3}$$

18. 7 kg of carrots and 5 kg of tomatoes cost a total of 480 p.

(4)

$$\text{Cost of 1 kg of carrots : cost of 1 kg of tomatoes} = 5 : 9$$

Work out the cost of 1 kg of carrots and the cost of 1 kg of tomatoes.

19. The menu in a restaurant has starters, main courses, and desserts.

(2)

- There are 5 starters.
- There are 12 main courses.
- There are  $x$  desserts.

There are 420 different ways to choose one starter, one main course, and one dessert.

Work out the value of  $x$ .

20. For  $x \geq 0$ , the functions  $f$  and  $g$  are such that

$$f(x) = 3x + 4 \text{ and } g(x) = \frac{\sqrt{x} + 2}{5}$$

(a) Find  $g^{-1}(x)$ .

(2)

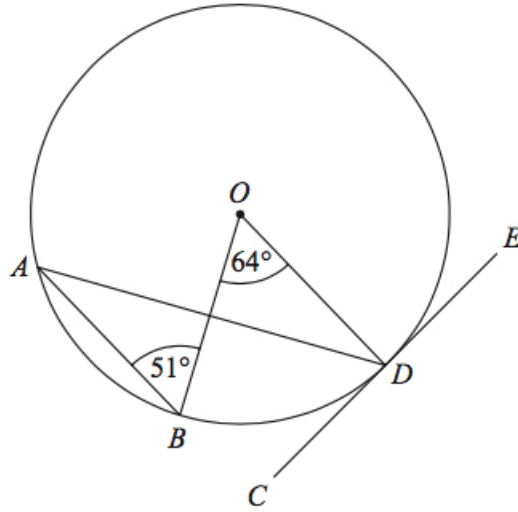
(b) Solve

(3)

$$gf(x) = 3.$$

21.  $A$ ,  $B$ , and  $D$  are points on a circle with centre  $O$ .  
 $CDE$  is the tangent to the circle at  $D$ .

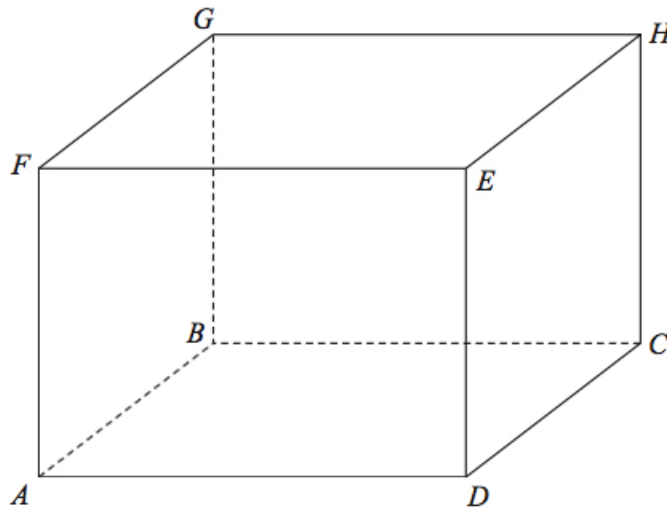
(4)



Work out the size of angle  $ADC$ .  
 Write down any circle theorems you use.

22.  $ABCDEFGH$  is a cuboid.

(2)



$AF = 6.8$  cm.  
 $FC = 13.6$  cm.

Work out the size of the angle between  $FC$  and the plane  $ABCD$ .



23. Write

(4)

$$\frac{3\sqrt{3}}{4 - \sqrt{3}} - \frac{2}{\sqrt{3}}$$

in the form

$$\frac{a\sqrt{3} + b}{c},$$

where  $a$ ,  $b$ , and  $c$  are integers.

24. Find the set of possible values of  $x$  for which

(5)

$$4x^2 - 25 < 0 \text{ and } 12 - 5x - 3x^2 > 0.$$

You must show all your working.

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